## Reading Assignment # 14

## Math 9 - Prof. Orellana

## Oct. 31, 2007 - Happy Halloween!

Read Section 13.3 and 13.4 and then answer the following questions.

- 1. What is the common question answered by Section 13.3 and 13.4?
- 2. Generalize the definition of dot product to vector in  $\mathbb{R}^n$ . What other names are used for dot product?
- 3. What are the properties of the dot product?
- 4. Read the proof of Theorem 3, now close the book and write a proof yourself.
- 5. What does it mean for two vectors in  $\mathbb{R}^n$  to be orthogonal?
- 6. What are the direction angles?
- 7. Define a vector projection and scalar projection and tell how they are related?
- 8. Write the definition of cross product? Now compare it with the dot product.
- 9. Based on the definition of  $2 \times 2$  and  $3 \times 3$  matrices, how would you generalize the determinant for a  $4 \times 4$  matrix?
- 10. Read the proof of Theorem 5 and then close the book and write the proof.
- 11. State Theorem 6 and tell me in your own words what you understand from it.
- 12. How can you test if two vectors in  $\mathbb{R}^3$  are parallel?
- 13. If **a** and **b** are two vectors, what is the length of  $\mathbf{a} \times \mathbf{b}$ ?
- 14. Explain figure 1, make sure to explain how is it related to the cross product.
- 15. What is the scalar triple product and what is its geometric significance?
- 16. What are the properties of the cross product? Is it associative?
- 17. Can you give a physics interpretation of the cross product? Explain.