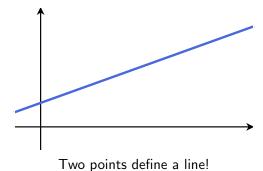
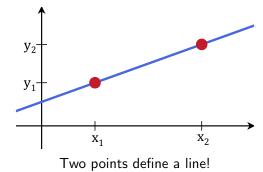
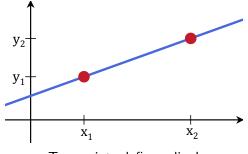
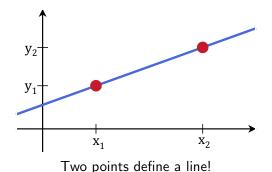
Functions and their graphs





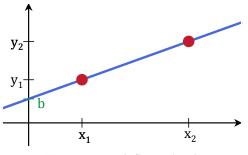


Slope:
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
 (rise/run)



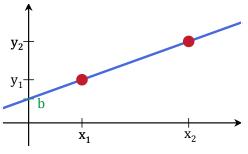
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 (rise/run)

Point-slope form: $y - y_1 = m(x - x_1)$ (good for writing down lines)



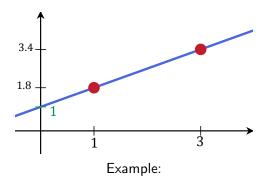
Two points define a line!

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General form: $Ax + By + C = 0$ (accounts for ∞ slope)



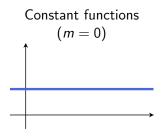
Slope:
$$m = \frac{3.4 - 1.8}{3 - 1} = 0.8$$
 (rise/run)

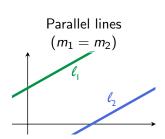
Point-slope form: y-1.8=0.8*(x-1) (good for writing down lines)

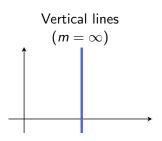
Slope-intercept form: y = 0.8 * x + 1 (good for graphing)

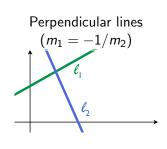
General form: 0.8 * x + y - 1 = 0 (accounts for ∞ slope)

Lines: Special cases









Other good functions to know: polynomials.

$$y = a_0 + a_1 x + \dots + a_n x^n$$

(n is the degree)

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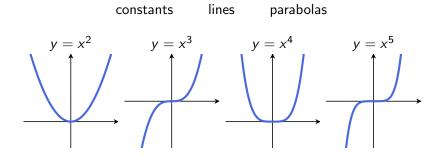
$$y = a_0 + a_1 x + \dots + a_n x^n$$

(n is the degree)

n = 0: n = 1:

n = 2:

The basics (know these graphs!)



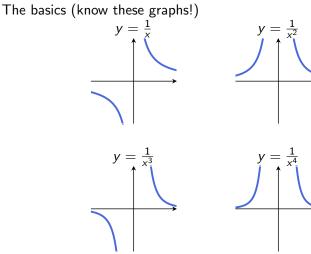
Other good functions to know: rationals.

$$y = \frac{a_0 + a_1 x + \dots + a_n x^n}{b_0 + b_1 x + \dots + b_m x^m}$$

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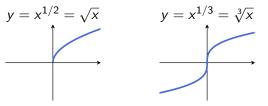
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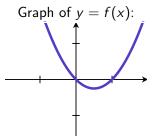
 $b_0 + b_1 x + \cdots + b_m x^m$

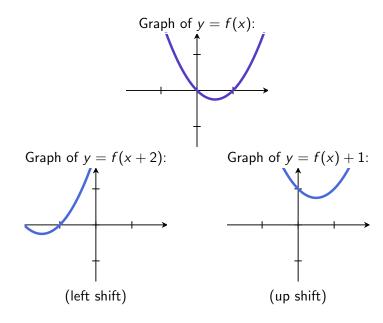


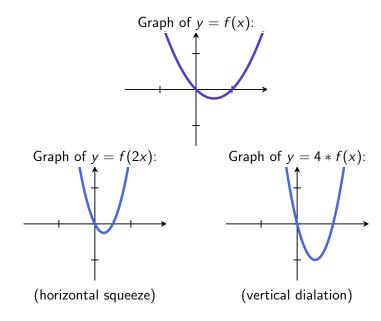
Other powers: $y = x^a$.

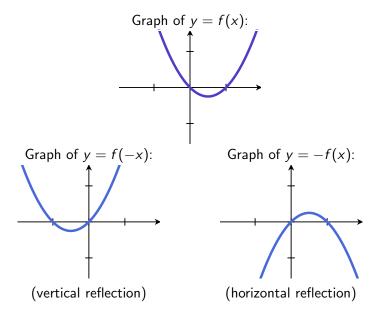
The basics (know these graphs!)

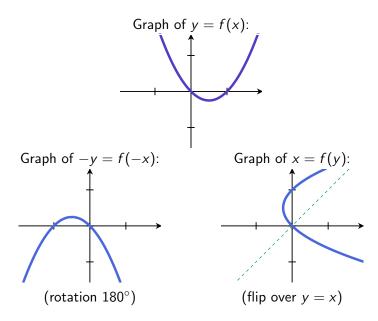






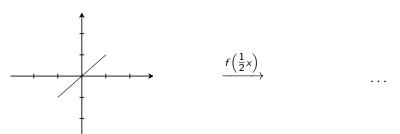






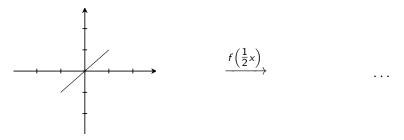
Example: See notes

Transform the graph of f(x) into the graph of $-f(\frac{1}{2}(x+1)) + 2$:



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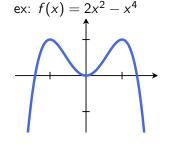


The *domain* of a function f is the set of x over which f(x) is defined. The *range* of a function f is the set of y which satisfy y = f(x) for some x.

Symmetries

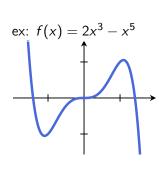
A function f(x) is even if it satisfies

$$f(-x)=f(x)$$

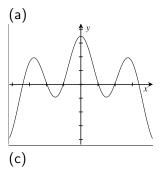


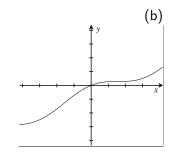
A function f(x) is *odd* if it satisfies

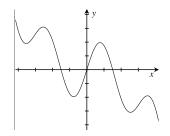
$$f(-x) = -f(x)$$

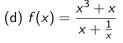


Examples: Even, odd, or neither?



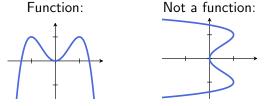




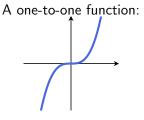


(for this one: actually plug in
$$-x$$
 and see what happens algebraically)

A graph is a graph of a *function* if for every x in its domain, there is exactly one y on the graph which is mapped to by that x:



A function is additionally *one-to-one* if for every y, there is at most one x which maps to that y.



Inverse functions

Let f be a one-to-one function. If g is a function satisfying

$$f(g(x)) = g(f(x)) = x$$

then g is the inverse function of f. Write $g(x) = f^{-1}(x)$.

To calculate $f^{-1}(x)$, set f(y) = x and solve for y. Then $y = f^{-1}(x)$.

To get the graph of $f^{-1}(x)$, flip the graph of f(x) over the line y = x.

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Example: If
$$f(x) = \frac{2x}{x-1}$$
,

solve
$$x = \frac{2y}{y-1}$$
 for y to get $y = \frac{x}{x-2}$.

So
$$f^{-1}(x) = \frac{x}{x-2}$$
.

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Pair up graphs with their inverses:

