THE LIMIT LAWS

1.
$$\lim_{x \to a} (f(x) + g(x)) = \lim_{x \to a} f(x) + \lim_{x \to a} g(x)$$

2.
$$\lim_{x \to a} (f(x) - g(x)) = \lim_{x \to a} f(x) - \lim_{x \to a} g(x)$$

3.
$$\lim_{x \to a} (f(x)g(x)) = \lim_{x \to a} f(x) \cdot \lim_{x \to a} g(x)$$

4.
$$\lim_{x \to a} (cf(x)) = c \lim_{x \to a} f(x)$$

5.
$$\lim_{x \to a} \frac{f(x)}{g(x)} = \frac{\lim_{x \to a} f(x)}{\lim_{x \to a} g(x)} \quad \text{if} \quad \lim_{x \to a} g(x) \neq 0$$

6.
$$\lim_{x \to a} (f(x))^n = \left(\lim_{x \to a} f(x)\right)^n$$

7.
$$\lim_{x \to a} c = c$$

$$8. \lim_{x \to a} x = a$$

9.
$$\lim_{x \to a} x^n = a^n$$

10.
$$\lim_{x\to a} \sqrt[n]{x} = \sqrt[n]{a}$$
 where n is a positive integer

11.
$$\lim_{x\to a} \sqrt[n]{f(x)} = \sqrt[n]{\lim_{x\to a} f(x)}$$
 where n is a positive integer

- 12. (Direct Substitution Property) If f is a polynomial or a rational function and a is in the domain of f, then $\lim_{x\to a} f(x) = f(a)$
- **13.** If $f(x) \leq g(x)$ when x is near a, then $\lim_{x \to a} f(x) \leq \lim_{x \to a} g(x)$
- 14. (The Squeeze Theorem) If $f(x) \leq g(x) \leq h(x)$ when x is near a and $\lim_{x \to a} f(x) = \lim_{x \to a} h(x) = L$, then $\lim_{x \to a} g(x) = L$ as well