

MATH 2 SOLUTIONS PROBLEM SET #3

SECTION 4.9

(2.) $f(x) = \frac{1}{2}x^2 - 2x + 6$

$$F(x) = \frac{1}{6}x^3 - x^2 + 6x + C$$

(6.) $f(x) = x(2-x)^2 = x^3 - 4x^2 + 4x$

$$F(x) = \frac{1}{4}x^4 - \frac{4}{3}x^3 + 2x^2 + C$$

(14.) $f(x) = 3e^x + 7\sec^2 x$

$$F(x) = 3e^x + 7\tan x + C$$

(18.) $f(x) = 2\sqrt{x} + 6\cos x = 2x^{\frac{1}{2}} + 6\cos x$

$$F(x) = \frac{4}{3}x^{\frac{3}{2}} + 6\sin x + C$$

(26.) $f''(x) = 6x + \sin x$

$$f'(x) = 3x^2 - \cos x + C$$

$$f(x) = x^3 - \sin x + Cx + D$$

(46.) $f'''(x) = \cos x$, $f(0) = 1$, $f'(0) = 2$, $f''(0) = 3$

$$f''(x) = \sin x + C_1 \quad f''(0) = 3 \Rightarrow C_1 = 3$$

$$f''(x) = \sin x + 3$$

$$f'(x) = -\cos x + 3x + C_2 \quad f'(0) = 2 \Rightarrow C_2 = 3$$

$$f'(x) = -\cos x + 3x + 3$$

$$f(x) = -\sin x + \frac{3}{2}x^2 + 3x + C_3 \quad f(0) = 1 \Rightarrow C_3 = 1$$

$$f(x) = -\sin x + \frac{3}{2}x^2 + 3x + 1$$

(over) ↗

(cont'd)

$$(58.) v(t) = 1.5\sqrt{t} = \frac{3}{2}t^{\frac{1}{2}}, \quad s(4) = 10.$$

$$s(t) = t^{3/2} + C$$

$$s(4) = 10 \Rightarrow 8 + C = 10 \Rightarrow C = 2$$

$$s(t) = \boxed{t^{3/2} + 2}.$$