

# Math 23 Diff Eq: Homework 4

due Wed Oct 19

Five of these are postponed from HW3. Sections 3.6 and 3.7 are the key parts to focus on this week, and might require a bit more time—be sure to attack them early!

**3.5:** 3, 14, 16, 21 (nice intuitive way to see why  $te^{rt}$  arises).

The next section suddenly involves more messy algebra (be prepared to keep track of lots of terms; use abbreviations to help, *e.g.*  $s$  and  $c$  for  $\sin \beta t$  and  $\cos \beta t$ ). The results are worth it though!

**3.6:** 1 (is  $e^{2t}$  a homog soln?), 2, 3 (is  $e^{-t}$  a homog soln? Use this info), 4, 14.

The next technique is equally crucial, but mainly boils down to evaluating two integrals each time:

**3.7:** 3 (important to get the two methods to agree—isn't it amazing how the  $t^2$  term emerges from variation of parameters?),

5 (look in integral table),

11 (simplify as much as you can),

13 (don't forget you can remove multiples of  $y_1$  and  $y_2$ , the homog solns, in the answer, and carefully choose lower limit  $t_0$ ),

23 (beautiful result for response of driven harmonic oscillator).

**3.8:** 1, 7, 12, 18.

**3.9:** 1, 17 (plot can be replaced by sketch but be sure to label some values, width/height of peak, etc)