Math 14<br>Winter 2009<br>Friday, January 23<br>Problems

(1.) Find the average $y$-coordinate of a point on the top half of the unit circle.
(2.) An object of mass $M$ located at the origin produces a gravitational field at point $(x, y)$ whose magnitude is $\frac{M G}{r^{2}}$ (where $G$ is a constant and $r$ is the distance to the origin) and whose direction is toward the origin.
(a.) Express the field at the point $(x, y)$ as a (vector) function $F(x, y)$.

Continued on reverse.
(b.) Find the average $x$ - and $y$-components of $F$ on the line segment from $(1,0)$ to $\left(1, \frac{\pi}{2}\right)$.

