

**Math 13 - Winter 2014**  
**Homework 2**  
Due Wednesday, 22 Jan. 2014.

**Note:**

- Except for problems that are stated explicitly, all problems are from Stewart Multi-variable Calculus 7th Edition.
- Please show all of your work (writing a list of answers is not sufficient).
- Please indicate the people you worked with.
- Please staple your page together.

1. Let  $\mathbf{v}_1$ ,  $\mathbf{v}_2$ , and  $\mathbf{v}_3$  be vectors in  $\mathbb{R}^3$ , where  $\mathbf{v}_1 = (1, 1, 1)$ ,  $\mathbf{v}_2 = (1, 1, 0)$ , and  $\mathbf{v}_3 = (1, 0, 0)$  and let  $L : \mathbb{R}^3 \rightarrow \mathbb{R}^3$  be the linear transformation such that

$$L(\mathbf{v}_1) = (2, -1, 4), \quad L(\mathbf{v}_2) = (3, 0, 1), \quad L(\mathbf{v}_3) = (-1, 5, 1)$$

Find the representing matrix of  $L$ , and use that matrix to find  $L(2, 4, -1)$ .

2. Section 15.1 (p. 1005) #4.
3. (**Corrected Jan 20, 2014**) If  $k$  is a constant  $f(x, y) = k$ , and  $R = [a, b] \times [c, d]$ , show that

$$\int \int_R k \, dA = k(b - a)(d - c).$$

4. Section 15.2 (p. 1011) #26.
5. Section 15.3 (p. 1020) #24.
6. In evaluating a double integral over a region  $D$ , a sum of iterated integrals was obtained as follows:

$$\int \int_D f(x, y) \, dA = \int_0^2 \int_0^{\sqrt{y}} f(x, y) \, dx dy + \int_2^4 \int_{y-2}^{\sqrt{y}} f(x, y) \, dx dy.$$

Sketch the region  $D$  and express the double integral as an iterated integral with reversed order of integration.