

- (1) Evaluate the integral  $\int \int_D \sqrt{x+2y} \sin(y-2x) dx dy$ , where  $D$  is the region bounded by the four lines  $y = 2x$ ,  $y = 2x + \frac{\pi}{2}$ ,  $x + 2y = 1$  and  $x + 2y = 9$ .
- (2) Consider the surface that is the part of the paraboloid  $z = x^2 + y^2 + 5$  with  $x \geq 0$  and  $y \geq 0$ , located between the planes  $z = 0$  and  $z = 9$ . Evaluate the scalar surface integral  $\iint \sqrt{1 + 4x^2 + 4y^2} dS$  over this surface.
- (3) Find the outward flux of the vector field  $\mathbf{F}(x, y, z) = (3xz^2, y, -z^3)$  across the surface of the solid in the first octant that is bounded by the surface  $x^2 + 4y^2 = 16$  and the planes  $y = 2z$ ,  $x = 0$ , and  $z = 0$ .
- (4) Find the area of the part of the graph of the function  $f(x, y) = xy$  that is outside the cylinder  $x^2 + y^2 = 1$  and inside  $x^2 + y^2 = 9$ .
- (5) Find the centroid of the region  $\{(x, y) : x^2 + y^2 \leq 1, x \geq 0, y \geq 0\}$  shaped like one fourth of a disk.
- (6) Find the area of the region enclosed by the curve  $\mathbf{x}(t) = (t^2, \frac{t^3}{3} - t)$ ,  $-\sqrt{3} \leq t \leq \sqrt{3}$ .
- (7) The force  $\mathbf{F}(x, y) = (y \cos x - y^3, \sin x - 3xy^2)$  acts on a particle as it moves from the point  $(0, 0)$  to the point  $(1, 1)$ , first along the horizontal line segment from  $(0, 0)$  to  $(1, 0)$ , and then along the vertical line segment from  $(1, 0)$  to  $(1, 1)$ . Find the work done.
- (8) Let  $C$  be the curve in the  $xy$ -plane consisting of the four sides of the square  $\{(x, y) : |x| \leq 1, |y| \leq 1\}$  oriented clockwise. Compute  $\oint_C (y^2 + z^2) dx + (x^2 + y^2) dy + (x^2 + y^2) dz$ .