

## Parametrizations of standard surfaces:

- Disk:  $(u, v) \rightarrow \langle r \cdot u \cos(v), r \cdot u \sin(v) \rangle$   $0 \leq v < 2\pi, 0 \leq u \leq 1$ .  $r$  is the radius.
- Elliptical Disk:  $(u, v) \rightarrow \langle r_1 \cdot u \cos(v), r_2 \cdot u \sin(v) \rangle$ , where  $r_1$  and  $r_2$  are the focal radii....that is to say that the ellipse that is the boundary has the equation  $\frac{x^2}{r_1^2} + \frac{y^2}{r_2^2} = 1$ .
- Sphere:  $(u, v) \rightarrow \langle r \cdot \sin(u) \cos(v), r \cdot \sin(u) \sin(v), r \cdot \cos(u) \rangle$ .  $r$  is the radius.
- Graph of surface  $f(x,y)$ :  $(u, v) \rightarrow \langle u, v, f(u, v) \rangle$ .

Surfaces bounded by cylinders and cones

- If the cylinder is of the form  $x^2 + y^2 = A$ , then parametrize, then we realize that the surface we want lies above the disk bounded by  $x^2 + y^2 = A$ . First parametrize this disk, and use that parametrization to parametrize the surface using the "graph" technique from above.
- If the bounding surface is a cone, attempt to find an equation given the boundary only in  $x$  and  $y$ , normally an elliptical disk. Parametrize that region, and then use the graph technique.