homework 5

1. Let $D$ be the triangular region drawn below.
a) Let $\rho_{0}(x, y)=1$. Compute the center of mass of $D$ and draw it in the diagram.
b) Let $\rho_{1}(x, y)=x$. Compute the center of mass of $D$ and draw it in the diagram.
c) Let $\rho_{2}(x, y)=x^{2}$. Compute the center of mass of $D$ and draw it in the diagram.
d) If you took $\rho(x, y)=x^{n}$ with higher and higher powers of $x$ how would the center of mass move?
2. Use polar coordinates to find the integral of the function $f(x, y)=x y$ over the region $D=\left\{(x, y) \mid 4 \leqslant x^{2}+y^{2} \leqslant 9, x \leqslant 0, y \geqslant 0\right\}$
