homework 5

1. Let D be the triangular region drawn below.

a) Let $\rho_0(x, y) = 1$. Compute the center of mass of D and draw it in the diagram.

b) Let $\rho_1(x, y) = x$. Compute the center of mass of D and draw it in the diagram.

c) Let $\rho_2(x, y) = x^2$. Compute the center of mass of D and draw it in the diagram.

d) If you took $\rho(x, y) = x^n$ with higher and higher powers of x how would the center of mass move?

2. Use polar coordinates to find the integral of the function f(x, y) = xy over the region $D = \{(x, y) | 4 \leq x^2 + y^2 \leq 9, x \leq 0, y \geq 0\}$