## Guts of a simple polyhedron: neighborhoods

Non-singular point:

Triple point:


Vertex:


A piece of a simple polyhedron


## Guts of a simple polyhedron: interior

## consists of

regions (or faces)


## Guts of a simple polyhedron: singular graph

consists of
edges,
vertices


## Construction of Bing's house

## main cubic building

## Construction of Bing's house

two rooms


## Construction of Bing's house

two tunnel entrances


## Construction of Bing's house

two extra walls for some luxury


## Strata of Bing's house

2 vertices

## Strata of Bing's house

2 vertices
2 edges

## Strata of Bing's house

2 vertices
2 edges
2 edges


## Strata of Bing's house

2 vertices
2 edges
2 edges
2 regions
+1 big region
$\chi=2-4+3=1$

Bing's house finished


## Interior of a room in Bing's house

## Thickening of a spine

## Stage 0:

original spine


## Thickening of a spine

## Stage 1:

vertices are inflated


## Thickening of a spine

## Stage 2:

edges are inflated


## Thickening of a spine

plates to glue


## Thickening of a spine

attaching "annuli"


## Thickening of a spine

## Stage 3:

final manifold


## Local moves of simple polyhedra



