

Let $S = \{(0, 1), (0, 2), (1, 2), (1, 3), (2, 0), (4, 1)\} \in \mathbb{R}^2$.

- (1) Draw $\text{conv}(S)$.
- (2) Is $\text{conv}(S)$ a polyhedron?
- (3) Is it true that $(3, 2) \in \text{conv}(S)$?
- (4) Is it true that $(2, 2) \in \text{conv}(S)$?
- (5) If you answered yes to any of the last two questions, prove it using the definition of $\text{conv}(S)$ (that is, express the point as a convex combination of points in S).