Hint for Problem 265-b

Why is it sufficient to focus on permutations that take vertex 1 to itself?