Hint for Problem 242-a

For each edge in F to connect two vertices of the same color, we must have all the vertices in a connected component of the graph with vertex set V and edge set F colored the same color.