Principles of Calculus Modeling: An Interactive Approach by Donald Kreider, Dwight Lahr, and Susan Diesel Exercises for Section 1.1

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1. ( 1 pt )

Calculate a few values to determine which image shows the graph of the function $4 x-3$.

2. $(1 \mathrm{pt})$

Calculate a few values to determine which image shows the graph of the function $-x+4$.

3. $(1 \mathrm{pt})$

Consider the following table of times and distances for a dropped object.

| time (x) | distance $(\mathbf{y})$ |
| :---: | :---: |
| 0 | 0 |
| 0.2 | 0.08 |
| 0.4 | 0.32 |
| 0.6 | $? ? ?$ |
| 0.8 | 1.28 |
| 1 | 2 |

If you assume the data points are modeled by a function of the form $y=a x^{2}+c$, which of the following values is most likely as the missing value in the table?
A. 0.08
B. 0.72
C. 7.2
D. 0
E. -0.72

## 4. (1 pt)

Consider the following table of times and distances for a dropped object.

| time (x) | distance $(\mathbf{y})$ |
| :---: | :---: |
| 0 | 1 |
| 3 | -53 |
| 6 | -431 |
| 9 | $? ? ?$ |
| 12 | -3455 |
| 15 | -6749 |

If you assume the data points are modeled by a function of the form $y=a x^{3}+c$, which of the following values is most likely as the missing value in the table?
A. -6749
B. -53
C. 1457
D. 0
E. -1457

## 5. ( 1 pt )

Consider a table of data.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 0 | 1.1 |
| 1 | -5.2 |
| 2 | -5.0 |
| 3 | -7.9 |
| 4 | -11.2 |
| 5 | -10.8 |

The data points in the table, and a line $L(x)$ passing among them, are shown below.


Assume the line passes through points $(0,1.1)$ and $(5,-10.8)$. Compute the sum of squared errors $\sum_{i=0}^{5}\left(y_{i}-L\left(x_{i}\right)\right)^{2}$.
6. $(1 \mathrm{pt})$

Consider a table of data.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 0 | 0.2 |
| 1 | -0.2 |
| 2 | -0.1 |
| 3 | 1.9 |
| 4 | 4.2 |
| 5 | 6.0 |

The data points in the table, and a line $L(x)$ passing among them, are shown below.


Assume the line passes through points $(0,0.2)$ and $(5,6.0)$. Compute the sum of squared errors $\sum_{i=0}^{5}\left(y_{i}-L\left(x_{i}\right)\right)^{2}$.
7. $(1 \mathrm{pt})$

Consider a table of data.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 0 | 0.1 |
| 1 | 0.3 |
| 2 | -0.3 |
| 3 | 0.7 |
| 4 | 1.5 |
| 5 | 5.1 |

The data points in the table, and a line $L(x)$ passing among them, are shown below.


Assume the line passes through points $(0,0.1)$ and $(5,5.1)$.
Compute the sum of squared errors $\sum_{i=0}^{5}\left(y_{i}-L\left(x_{i}\right)\right)^{2}$.
8. $(1 \mathrm{pt})$

Let $f(x)=-3 \sin (8 x)-1$. Compute $f(x)$ for the following values. If $f(x)$ cannot be evaluated, enter no answer, without quotes.

$$
f(0)=
$$

$\qquad$
$f(-1)=$ $\qquad$
$f(1)=$
$f(\sqrt{2})=$ $\qquad$
$f(e)=$ $\qquad$
9. $(1 \mathrm{pt})$

Let $f(x)=-7 \frac{\sqrt{10-x}}{x^{2}}$. Compute $f(x)$ for the following values. If $f(x)$ cannot be evaluated, enter no answer, without quotes.

$$
\begin{aligned}
& \quad f(0)= \\
& f(-1)= \\
& f(13)= \\
& f(\sqrt{2})= \\
& f(e)= \\
& \hline
\end{aligned}
$$

10. (1 pt)

Let $f(x)=8 x^{2}+4 x+2$. Compute $f(x)$ for the following values. If $f(x)$ cannot be evaluated, enter no answer, without quotes.
$f(0)=$ $\qquad$
$f(-1)=$ $\qquad$
$f(9)=$
$f(\sqrt{2})=$ $\qquad$
$f(e)=$ $\qquad$
11. (1 pt)

Consider the following table of data values.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 3 | 18 |
| 6 | 43 |
| 9 | 90 |
| 12 | 154 |
| 15 | 233 |
| 18 | 333 |

Which of the following functions best fits the data given in the table?
A. $y=3 x^{2}+3$
B. $y=2 x^{2}+7$
C. $y=1 x^{2}+9$
D. $y=11$

## 12. ( 1 pt )

Consider the following table of points.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 0 | 7.5 |
| 1 | 14 |
| 2 | 33.5 |
| 3 | 66 |

If the points in the table are on a curve of the form $y=a x^{2}+c$, then what are the values of $a$ and $c$ ?
$a=$ $\qquad$
$c=$
13. $(1 \mathrm{pt})$

Consider the following table of data values.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :--- |
| 0 | 10 |
| 2 | 16 |
| 4 | 22 |
| 6 | 18 |

For each of the following lines $y=m x+b$, calculate the sum of squared errors $\sum_{i=0}^{3}\left(y_{i}-\left(m x_{i}+b\right)\right)^{2}$.

$$
y=3 x+10
$$

Sum of squared errors: $\qquad$

$$
y=3 x+6
$$

Sum of squared errors: $\qquad$

$$
y=1 x+8
$$

Sum of squared errors: $\qquad$

According to the values you just computed, which of the following lines best fits the data?
A. $y=3 x+10$
B. $y=3 x+6$
C. $y=1 x+8$
14. (1 pt)

Consider the following table of points.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 0 | 17.00 |
| 1.5 | -3.92 |
| 3 | -150.40 |
| 4.5 | -547.98 |
| 6 | -1322.20 |
| 7.5 | -2598.62 |

If the points in the table are on a curve of the form $y=a x^{3}+c$, then what are the values of $a$ and $c$ ?
$a=$ $\qquad$
$c=$
15. $(1 \mathrm{pt})$

Consider the following table of data values.

| $\mathbf{x}$ | $\mathbf{y}$ |
| :---: | :---: |
| 0 | 19 |
| 4.2 | 76.74 |
| 8.4 | 267.96 |
| 12.6 | 580.66 |

For each of the following functions $y=a x^{2}+c$, calculate the sum of squared errors $\sum_{i=0}^{3}\left(y_{i}-\left(a x_{i}^{2}+c\right)\right)^{2}$.

$$
y=4.5 x^{2}+19
$$

Sum of squared errors: $\qquad$
$y=3.5 x^{2}+15$
Sum of squared errors: $\qquad$

$$
y=2.5 x^{2}+17
$$

Sum of squared errors: $\qquad$
According to the values you just computed, which of the following functions best fits the data?
A. $y=4.5 x^{2}+19$
B. $y=3.5 x^{2}+15$
C. $y=2.5 x^{2}+17$

