

# HW 2

1.4 4.  $Ax = \begin{bmatrix} 8 & 3 & -4 \\ 5 & 1 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = 1 \cdot \begin{bmatrix} 8 \\ 5 \end{bmatrix} + 1 \cdot \begin{bmatrix} 3 \\ 1 \end{bmatrix} + 1 \cdot \begin{bmatrix} -4 \\ 2 \end{bmatrix} = \begin{bmatrix} 7 \\ 8 \end{bmatrix}$

(2 points)  $Ax = \begin{bmatrix} 8 & 3 & -4 \\ 5 & 1 & 2 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 8 \cdot 1 + 3 \cdot 1 + (-4) \cdot 1 \\ 5 \cdot 1 + 1 \cdot 1 + 2 \cdot 1 \end{bmatrix} = \begin{bmatrix} 7 \\ 8 \end{bmatrix}$

10.  $x_1 \begin{bmatrix} 8 \\ 5 \\ 1 \end{bmatrix} + x_2 \begin{bmatrix} -1 \\ 4 \\ -3 \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 2 \end{bmatrix}$ , and  $\begin{bmatrix} 8 & -1 \\ 5 & 4 \\ 1 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 4 \\ 1 \\ 2 \end{bmatrix}$

14. No. The equation  $Ax = u$  has no solution.  
(3 points)

15. The equation is not consistent when  $3b_1 + b_2$  is not zero.

The set of  $b$  for which the equation is consistent is a line through the origin - the set of all points  $(b_1, b_2)$  satisfying  $b_2 = -3b_1$ .

24 (3 points) (a) True. see 1.4 theorem 3

(b) True. Example 2

(c) True. Theorem 3

(d) True. See the box before example 2.

(e) False. see "warning" that follows theorem 4.

(f) True. see Theorem 4.

1.5 6  $x = x_3 \begin{bmatrix} -4 \\ 3 \end{bmatrix}$   
(3 points)

16 (3 points)  $x = \begin{bmatrix} 5 \\ 8 \end{bmatrix} + x_3 \begin{bmatrix} -4 \\ 3 \end{bmatrix} = p + x_3 q$ . The solution set is the line through  $p$ , parallel to  $q$ .

24 (2 points) (a) False. A nontrivial solution of  $Ax = 0$  is any nonzero  $x$  that satisfied the equation

(b) True. see example 2.

(c) True. If the zero vector is a solution, then  $b = Ax = A0 = 0$

(d) True. See the paragraph following example 3.

(e) False. Theorem 6 applies only to a consistent system.

most people got this wrong

1.6 11 (2 points)  $\left. \begin{array}{l} x_1 = 20 - x_3 \\ x_2 = 60 + x_3 \\ x_3 \text{ is free} \\ x_4 = 60 \end{array} \right\}$  Since  $x_1$  is non-negative, the largest value of  $x_3$  is 20.

12 (3 points + bonus 2 pts) (a)  $\left. \begin{array}{l} x_1 = 100 + x_3 - x_5 \\ x_2 = 100 - x_3 + x_5 \\ x_3 \text{ is free} \\ x_4 = 60 - x_5 \\ x_5 \text{ is free.} \end{array} \right\}$  (b)  $\left. \begin{array}{l} x_1 = 40 + x_3 \\ x_2 = 160 - x_3 \\ x_3 \text{ is free} \\ x_4 = 0 \\ x_5 = 60 \end{array} \right\}$  (c) Minimum value of  $x_1$  is 40 cars/minute.

1.7 (2) Linearly independent. (2 points)

8. Linearly dependent since there are more variables than equations. (3 points)

10 (3 point) (a)  $\left[ \begin{array}{ccc} 1 & -2 & 2 \\ -5 & 10 & -9 \\ -3 & 6 & k \end{array} \right]$  as augmented matrix is inconsistent.

Thus no  $k$  satisfies the requirement.

(b). All  $k$  satisfy the requirement.

22 (3 points) (a) True. see fig 1

(b) False. see "warning" after Theorem 8.

(c) True. see "remark" after Example 4.

(d). False. see example 3(a)

1.8 8. 4 columns and 5 rows.

11 (2 points) Yes, because the system represented by  $[A \ b]$  is consistent.

18 (2 points) Note that  $w = 2v + u$

